Quiz #8 MATH 54, Fall 2016, Section 219

Name: _		
Section:		

1. Let

$$A = \begin{bmatrix} 5 & -4 & -2 \\ -4 & 5 & 2 \\ -2 & 2 & 2 \end{bmatrix}.$$

Using the fact that $\mathbf{v}_1 = (-2, 2, 1)^T$ and $\mathbf{v}_2 = (1, 1, 0)^T$ are eigenvectors for A, find an orthogonal basis for \mathbb{R}^3 consisting of eigenvectors for A. (Hint: You don't need to solve the characteristic equation or find eigenspaces in this problem.)

2. Let $\mathcal{A} = \{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$ and $\mathcal{B} = \{\mathbf{u}_1, \mathbf{u}_2, \mathbf{u}_3\}$ be two bases for a vector space V, and suppose

$$\mathbf{u}_1 = 2\mathbf{v}_1 - 3\mathbf{v}_2 + \mathbf{v}_3, \quad \mathbf{u}_2 = 3\mathbf{v}_1 - \mathbf{v}_2, \quad \mathbf{u}_3 = -\mathbf{v}_2 + \mathbf{v}_3.$$

Let $\mathbf{v} = \mathbf{u}_1 + \mathbf{u}_2 + \mathbf{u}_3$. Find $[\mathbf{v}]_{\mathcal{A}}$.